

SE for k ratio in APIM using the first order delta method

$$k = p/a$$

$$\begin{aligned}
 SE_{p/a} &= \sqrt{\begin{bmatrix} 1 & -p \\ a & a^2 \end{bmatrix} \begin{bmatrix} s_p^2 & s_{pa} \\ s_{pa} & s_a^2 \end{bmatrix} \begin{bmatrix} 1 \\ a \\ -p \\ a^2 \end{bmatrix}} = \sqrt{\begin{bmatrix} s_p^2 - \frac{ps_{pa}}{a} & s_{pa} - \frac{ps_a^2}{a} \\ s_{pa} - \frac{ps_a^2}{a} & -\frac{p}{a^2} \end{bmatrix} \begin{bmatrix} 1 \\ a \\ -p \\ a^2 \end{bmatrix}} = \sqrt{\frac{s_p^2}{a^2} - \frac{ps_{pa}}{a^3} - \frac{ps_{pa}}{a^3} + \frac{p^2 s_a^2}{a^4}} \\
 &= \sqrt{\frac{s_p^2}{a^2} - \frac{2ps_{pa}}{a^3} + \frac{p^2 s_a^2}{a^4}}
 \end{aligned}$$

a = unstandardized actor effect,

p = unstandardized partner effect

s_a^2 = variance (SE^2) actor effect

s_p^2 = variance (SE^2) partner effect

s_{pa} = covariance between actor and partner effect